Die Moleküle ordnen sich in Schichten parallel zur $a c$-Ebene an. Innerhalb dieser Schichten besteht eine dichteste Kugelpackung der Molekülschwerpunkte.*

Diese Arbeit wurde von der Deutschen Forschungsgemeinschaft, dem Fonds der Chemischen Industrie und der Badischen Anilin- \& Sodafabrik unterstützt. Für diese hochherzige Förderung sprechen wir unseren besten Dank aus.

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* Inzwischen wurde die Bullvalenstruktur auch von anderer Seite unabhängig gelöst. Soweit aus der Kurzmitteilung (Johnson. McKechnie, Lin \& Paul, 1967) zu ersehen ist, sind beide Ergebnisse identisch.

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# Crystal Structure of a High-Pressure Form of $\mathrm{B}_{2} \mathrm{O}_{3}$ 

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(Received 11 July 1967)
$\mathrm{B}_{2} \mathrm{O}_{3}$ II is a high-pressure phase of boron oxide first reported by Dachille \& Roy. Crystals for this work were grown in a tetrahedral anvil at 65 kbar and $1100^{\circ} \mathrm{C}$ and quenched to room temperature. The crystals are orthorhombic with $a=4.613 \pm 0.001, b=7.803 \pm 0.002, c=4.129 \pm 0.001 \AA, Z=4$, $\mathrm{D}_{o}=3 \cdot 14, D_{c}=3 \cdot 11 \mathrm{g.cm}{ }^{-3}$, space group $C c m 2_{1}$, and are weakly piezoelectric. The structure, which has been refined by least squares, consists of a network of corner-linked $\left(\mathrm{BO}_{4}\right)^{5-}$ tetrahedra. Within each tetrahedron there are three long B-O distances of $1.507,1.506$, and $1.512 \AA$, and one short distance of $1.373 \AA$. The oxygen associated with the short distance is coordinated by only two boron atoms, whereas the other is coordinated by three boron atoms. Unlike the low-pressure hexagonal form, $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}, \mathrm{B}_{2} \mathrm{O}_{3} \mathrm{II}$ is relatively unaffected by hot water or hot concentrated hydrochloric acid. It can be heated in air to just below its melting point without reverting to the ambient pressure structure. In addition, the density of $\mathrm{B}_{2} \mathrm{O}_{3}$ II is greater by $27 \%$ ( $3 \cdot 11 \mathrm{vs} .2 \cdot 44$ ). Another phase reported by Dachille \& Roy was also present in the product from the high-pressure runs. This fine-grained material is cubic with $a=8.914$ and is probably cubic metaboric acid ( $\%-\mathrm{HBO}_{2}$ ).

## Introduction

The high-pressure form of $\mathrm{B}_{2} \mathrm{O}_{3}$ was reported by Da chille \& Roy (1959) who first synthesized this material in a Bridgman uniaxial device at 35 kbar and $525^{\circ} \mathrm{C}$. Dachille \& Roy and, subsequently, Mackenzie \& Claussen (1961) prepared phase diagrams which show the lower pressure limits for synthesis to be about 20 kbar . Although the compounds produced in both investigations appeared to be identical, there were certain inconsistencies and no attempt was made to solve the crystal structure of the new form.

Because of the uncertainty surrounding the nature of high-pressure $\mathrm{B}_{2} \mathrm{O}_{3}$ and, indeed, of the whole $\mathrm{B}_{2} \mathrm{O}_{3}$ system, we grew crystals of the high-pressure phase and

[^0]solved the crystal structure with X-ray diffraction methods. This paper is a report of this investigation.

## Previous work

Without making an exhaustive survey of previous investigations of $\mathrm{B}_{2} \mathrm{O}_{3}$, it is interesting to trace the history of attempts to synthesize and characterize the crystalline material. Apparently Cole \& Taylor (1935) were the first to report diffraction data on a crystalline phase of $\mathrm{B}_{2} \mathrm{O}_{3}$ which they made by heating $\mathrm{H}_{3} \mathrm{BO}_{3}$ under vacuum at $200^{\circ} \mathrm{C}$ and then sintering at higher temperatures up to $290^{\circ} \mathrm{C}$. The product was cubic with $a=10.03 \AA, D_{o}=1.805 \mathrm{g.cm}{ }^{-3}$, and $D_{c}=1.818 \mathrm{~g} . \mathrm{cm}^{-3}$. The density of $\mathrm{B}_{2} \mathrm{O}_{3}$ glass as reported by Cole \& Taylor is $1.844 \mathrm{~g} . \mathrm{cm}^{-3}$, which is higher than the density of this cubic phase. Later authors have discounted the

Cole \& Taylor work, however, assuming that their product was not really $\mathrm{B}_{2} \mathrm{O}_{3}$. Kracek, Morey \& Merwin (1938) and McCulloch (1939) independently prepared crystalline forms of $\mathrm{B}_{2} \mathrm{O}_{3}$ by heating $\mathrm{H}_{3} \mathrm{BO}_{3}$ in open containers for very long periods at temperatures around $240^{\circ} \mathrm{C}$. Berger (1953) has proposed a structure for this material which is hexagonal with $a=4 \cdot 334, c=8 \cdot 334 \AA$, $D_{o}=2.44 \mathrm{~g} . \mathrm{cm}^{-3}$, and $D_{c}=2.56 \mathrm{~g} . \mathrm{cm}^{-3}$.

An interesting investigation of crystallization phenomena and the effect of high pressure on $\mathrm{B}_{2} \mathrm{O}_{3}$ has been conducted by Uhlmann, Hays \& Turnbull (1967). In this work the ' $\mathrm{B}_{2} \mathrm{O}_{3}$ crystallization anomaly' was defined. This anomaly is that it has been impossible to grow crystals of $\mathrm{B}_{2} \mathrm{O}_{3}$ at atmospheric pressure from a dry $\mathrm{B}_{2} \mathrm{O}_{3}$ melt, even when the melt was seeded with $\mathrm{B}_{2} \mathrm{O}_{3}$ I crystals.
Since it is possible that both low-pressure forms have legitimate $\mathrm{B}_{2} \mathrm{O}_{3}$ structures, it may be necessary at some time to alter the following naming conventions. In this paper, the low-pressure hexagonal phase will be called $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$ and the high-pressure one $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{II}$, corresponding to Mackenzie \& Claussen's $\alpha-\mathrm{B}_{2} \mathrm{O}_{3}$ and $\beta-\mathrm{B}_{2} \mathrm{O}_{3}$, respectively. The latter convention is not a good one for naming pressure-related polymorphs and is therefore not followed in this paper.

## Experimental

The high-pressure experiments were performed in a manner similar to that of Bither, Gillson \& Young (1966) and Shannon (1967). Each powdered sample was pressed at $20,000 \mathrm{lb} . \mathrm{in}^{-2}$ into a small pellet and placed in a cylindrical Pt capsule. This assembly was placed in the center of a pyrophyllite tetrahedron, pressurized to 65 kbar , held at temperature for 1 hr , and quenched. The Pt capsule was used as its own heater; rapid quenching was achieved by cutting off the power. Since an estimated gradient of $100-300^{\circ} \mathrm{C}$ existed from the center to the ends of the capsule, samples were not necessarily homogeneous.

Several starting materials were used. The first was a mixture which had previously been prepared as a possible fluorescent host by Borchardt (1967). This mixture, which consisted of $98 \% \mathrm{~B}_{2} \mathrm{O}_{3}$ (Baker purified) and $2 \% \mathrm{Eu}_{2} \mathrm{O}_{3}$ (Lindsay $99 \cdot 9 \%$ ), was heated at $700^{\circ} \mathrm{C}$ for 4 hr in air. The X-ray powder pattern indicated (1) the major phase to be identical with an unindexed phase reported by Senkovits \& Hawley* as $\mathrm{B}_{2} \mathrm{O}_{3}$ and (2) a minor phase to be $\mathrm{EuBO}_{3}$. This mixture, after pressurizing to 65 kbar at $800^{\circ} \mathrm{C}$ was a gray, translucent sintered pellet. An X-ray powder pattern from this pellet showed no trace of the starting materials, $\mathrm{B}_{2} \mathrm{O}_{3} . n \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{EuBO}_{3}$; however, many of the strong lines in the powder pattern corresponded to the high-

[^1]pressure phase of $\mathrm{B}_{2} \mathrm{O}_{3}$ reported by Dachille \& Roy (1959).

A second source was Baker purified $\mathrm{B}_{2} \mathrm{O}_{3}$. Thermogravimetric analysis of this ' $\mathrm{B}_{2} \mathrm{O}_{3}$ ' showed a $17 \cdot 3 \%$ weight loss from $80-350^{\circ} \mathrm{C}$ which was presumably from water of hydration. In an attempt to grow crystals of $\mathrm{B}_{2} \mathrm{O}_{3}$ II this material was heated at $1200^{\circ} \mathrm{C}$ ( 65 kbar ) and quenched. The center of the capsule contained large, transparent, colorless crystals whose X-ray pattern could be indexed as cubic with a cell edge of $8.901 \AA$. This material is probably cubic metaboric acid ( $\gamma-\mathrm{HBO}_{2}$ ) whose reported cell edge is $8.886 \AA$ (Zachariasen, 1963a). These crystals dissolved rapidly in $\mathrm{H}_{2} \mathrm{O}$.

At the cold end of the capsule, transparent colorless crystals, $\frac{1}{2} \times \frac{1}{2} \mathrm{~mm}$, of $\mathrm{B}_{2} \mathrm{O}_{3}$ II were found. These crystals were insoluble in hot water and hot concentrated hydrochloric acid. The density of these crystals, as determined by the displacement method in bromoform, was $3 \cdot 14$. The crystals, observed under a hot stage microscope, showed melting at $525^{\circ} \mathrm{C}$. This observed melting point was confirmed by (1) a high temperature X-ray powder diffraction pattern which showed no change up to a temperature of $525^{\circ} \mathrm{C}$, and (2) an endothermic differential thermal analysis peak at $550^{\circ} \mathrm{C}$. Mackenzie \& Claussen (1961) noted melting of $\mathrm{B}_{2} \mathrm{O}_{3}$ II at $475-520^{\circ} \mathrm{C}$, depending on heating rate. $\mathrm{B}_{2} \mathrm{O}_{3}$ II was found to be an insulator with a room-temperature resistivity of $2 \times 10^{9} \mathrm{ohm}-\mathrm{cm}$, as measured by the fourprobe technique described by Bither et al. (1966). Hardness measurements carried out on a Wilson Tukon testing machine with three crystals of $\mathrm{B}_{2} \mathrm{O}_{3}$ II embedded in 'Lucite' ${ }^{\text {® }}$ acrylic resin resulted in values of $\mathrm{KHN}_{25}$ of $900-1000 \mathrm{~kg} . \mathrm{mm}^{-2}$. Hardness of materials synthesized at high pressures should be greater because of defects introduced in the process. Therefore, these values represent an upper limit to the hardness. Furthermore there is some question as to hardness determined on samples embedded in 'Lucite' $\Theta$.

A final experiment was performed by heating anhydrous Baker purified $\mathrm{B}_{2} \mathrm{O}_{3}$ to $1200^{\circ} \mathrm{C}$ at 65 kbar and cooling at $100^{\circ} \mathrm{C}$ per hr to $400^{\circ} \mathrm{C}$ where the specimen was quenched. The entire sample was found to be $\mathrm{B}_{2} \mathrm{O}_{3}$ II.

Cell dimensions for $\mathrm{B}_{2} \mathrm{O}_{3}$ II from a least-squares refinement ( 13 observations) of de Wolff-Guinier photograph data are $a=4 \cdot 613 \pm 0.001, b=7 \cdot 803 \pm 0.002, c=$ $4.129 \pm 0.001 \AA$, with $V=148.64 \AA^{3}, Z=4, D_{o}=3 \cdot 14$, $D_{c}=3.11 \mathrm{g.cm}^{-3}$. and $\mu(\mathrm{Cu} K \alpha)=27.3 \mathrm{~cm}^{-1}$. The space group, determined from precession photographs and a positive test for piezoelectricity, is $\mathrm{Ccm} 2_{1}$. Mackenzie \& Claussen (1961) reported a monoclinic cell with $a=4 \cdot 52, b=4 \cdot 14, c=4 \cdot 64$, and $\beta=120^{\circ} 25^{\prime}$.

This latter cell can be related to the orthorhombic cell by the transformation

$$
\begin{aligned}
& \mathbf{a}_{\otimes}=\mathbf{c}_{m} \\
& \mathbf{b}_{o}=2 \mathbf{a}_{m}+\mathbf{c}_{m} \\
& \mathbf{c}_{o}=\mathbf{b}_{m}
\end{aligned}
$$

Close examination of Weissenberg and precession photographs, plus the refinement results, indicate that the orthorhombic cell is the correct choice.

## Crystal structure and refinement

A structure for $\mathrm{B}_{2} \mathrm{O}_{3}$ II was proposed from consideration of the space group and the probability that the oxygen atoms were in a closest-packed arrangement. To test this hypothesis, all available reflections were collected with a Picker automatic diffractometer, using Ni -filtered $\mathrm{Cu} K \alpha$ radiation and a scintillation detector with pulse-height analysis. Each peak was integrated at a scan speed of $1^{\circ}$ per minute, with 40 -second backgrounds at the extremes of each scan. The intensities were converted to structure factors using a computer program, ACACA, written by Prewitt (1966a) which uses the Wuensch \& Prewitt (1965) method for calculating absorption corrections. Although the crystal shape was somewhat irregular, it was approximated by a rectangular prism of dimensions $0 \cdot 11 \times 0 \cdot 15 \times 0 \cdot 23$ mm . At this stage the Zachariasen (1963c) secondary extinction parameter $\beta$ was calculated for use later in the least-squares refinement. Sigmas for each reflection were computed with the use of

$$
\sigma_{F^{\prime}}=(\operatorname{Lp} T)^{-\frac{1}{2}}\left[\left(I+\sigma_{I}\right)^{\frac{1}{2}}-I^{\frac{1}{2}}\right]
$$

where $\mathrm{L}, \mathrm{p}$, and $T$ are the Lorentz, polarization, and transmission factors, respectively, $I$ is the integrated intensity, and

$$
\sigma_{I}=\left[E+\binom{T_{E}}{2 T_{B}}^{2}\left(B_{1}+B_{2}\right)+\varepsilon^{2} I^{2}\right]^{\frac{1}{2}}
$$

Here $E$ is the total count plus background, $T_{E}$ and $T_{B}$ are peak and background times, $B_{1}$ and $B_{2}$ are background counts, and $\varepsilon$, set in this case to $0 \cdot 03$, is to account for fluctuations in direct beam intensity. In all, 462 reflections were collected. These reflections and their $\sigma$ 's were subsequently reduced to a unique set of 81 reflections.

After a preliminary structure factor calculation indicated the proposed structure was correct, this structure was refined with a full-matrix, least-squares program written by Prewitt (1966b). In this program the quantity minimized is $\Sigma w\left|\left|F_{o}\right|-\left|F_{c}\right|\right|^{2}$ and the discrepancy index, $R$, is equal to $\Sigma\left|\left|F_{o}\right|-\left|F_{c}\right|\right| / \Sigma\left|F_{o}\right|$. Several cycles of refinement of scale factor, positional parameters, and isotropic temperature factors reduced $R$ to 0.079 but resulted in negative temperature factors for all atoms. At this point the secondary extinction parameter, $C$, where $F_{\text {corr }}=F_{o}\left[1+\beta C I_{o}\right]$, was varied, which resulted in reasonable isotropic temperature factors. After further cycles with all parameters varied, including anisotropic temperature factors, the unweighted $R$ for all reflections was 0.028 and the weighted $R$ was 0.034 . Examination of structure factors at this stage of refinement showed that the strongest reflections were still affected by extinction. Therefore, another cycle was run in which the twelve reflections for which
$\beta C I_{o}>0.25$ were not included. Although the change in positional parameters was negligible, there were small shifts in the orientations of the thermal vibration ellipsoids. Both the unweighted and weighted $R$ 's were 0.022 for the reflections included in the last cycle. $R$ for all reflections was 0.031 . Atomic scattering factors used for the refinement to this point were the curves for neutral B and O taken from International Tables for X-ray Crystallography (1962). Two more cycles were run with the curve for $\mathrm{B}^{3+}$ from International Tables and that for $\mathrm{O}^{2-}$ from Tokonami (1965). The latter results were not significantly different from those for which neutral B and O curves were used.

Table 1 gives the final observed and calculated structure factors. Table 2 gives a list of the final refined parameters obtained from the 'neutral scattering factor' cycle with $R=0 \cdot 022$. Table 3 is a compilation of the magnitudes and orientations of the thermal vibration ellipsoids. The values in Table 3 and the distances and angles in Table 4 were obtained with the Busing, Martin \& Levy (1962) program ORFFE.

Table 1. Observed and calculated structure factors
Quantities given are $h, k, l, 100 F_{o}$, and $100 F_{c}$. Reflections not included in final cycle of refinement are marked with *.


Table 2. Final atom parameters* for $\mathrm{B}_{2} \mathrm{O}_{3}$ II
Standard deviations are in parentheses.
The temperature factors are the coefficients in the expression $\exp \left\{-\left(\beta_{11} h^{2}+\beta_{22} k^{2}+\beta_{33} /^{2}+2 \beta_{12} h k+2 \beta_{13} h l+2 \beta_{23} k l\right)\right\}$ For $O(1), \beta_{12}=\beta_{23}=0$.

|  | B | $\mathrm{O}(1)$ | $\mathrm{O}(2)$ |
| :--- | :---: | :--- | :--- |
|  | $0.1606(4)$ | $0.2475(3)$ | $0.3698(3)$ |
| $x$ | $0.1646(3)$ | 0 | $0.2911(1)$ |
| $y$ | $0.335(9)$ | 0.5 | $0.5802(8)$ |
| $z$ | $0.007(1)$ | $0.003(1)$ | $0.0085(9)$ |
| $\beta_{11}$ | $0.0017(4)$ | $0.0026(4)$ | $0.0015(3)$ |
| $\beta_{22}$ | $0.07(1)$ | $0.011(1)$ | $0.005(1)$ |
| $\beta_{33}$ | $0.0002(5)$ | 0 | $0.0006(3)$ |
| $\beta_{12}$ | $-0.0015(9)$ | $-0.0003(5)$ | $-0.0001(6)$ |
| $\beta_{13}$ | $-0.0009(5)$ | 0 | $-0.0004(4)$ |
| $\beta_{23}$ | 0.45 | 0.55 | 0.49 |
| $B_{\text {eq }}$ | 0.57 | 0.26 | 0.72 |
| $B_{11}$ | 0.42 | 0.62 | 0.37 |
| $B_{22}$ | 0.36 | 0.76 | 0.37 |
| $B_{33}$ | 0.33 | 0.00 | 0.08 |
| $B_{12}$ | -0.12 | -0.02 | -0.01 |
| $B_{13}$ | 0.12 | 0.00 | -0.05 |
| $B_{23}$ | 0.12 |  |  |

Table 3. Magnitudes and orientations of thermal ellipsoids

|  |  | Standard deviations are in parentheses. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | r.m.s. | Angles with respect to |  |  |
|  |  | amplitude | $a$ | b | $c$ |
| B | $r_{1}$ | 0.06 (1) $\AA$ A | 76 (15) ${ }^{\circ}$ | $58(17)^{\circ}$ | 36 (12) ${ }^{\circ}$ |
|  | $r_{2}$ | 0.076 (8) | 59 (18) | 142 (19) | 69 (19) |
|  | $r_{3}$ | 0.091 (7) | 35 (18) | 71 (16) | 118 (12) |
| $\mathrm{O}(1)$ | $r_{1}$ | 0.06 (1) | 2 (5) | 90 | 88 (5) |
|  | $r_{2}$ | 0.089 (7) | 90 | 0 | 90 |
|  | $r_{3}$ | 0.098 (6) | 92 (5) | 90 | 2 (5) |
| $\mathrm{O}(2)$ | $r_{1}$ | 0.069 (9) | 98 (8) | 40 (25) | 51 (27) |
|  | $r_{2}$ | 0.072 (7) | 80 (8) | 127 (26) | 39 (27) |
|  | $r_{3}$ | $0 \cdot 097$ (5) | 13 (7) | 77 (6) | 93 (7) |

Table 4. Interatomic distances and interbond angles

| Standard deviations are in parenthe |  |
| :---: | :---: |
| $\mathrm{B}-\mathrm{O}(1)$ | 1.373 (3) $\AA$ |
| -O(2) | 1.507 (2) |
| -O(2') | 1.506 (3) |
| -O(2') | 1.512 (2) |
| O(ave) | 1.475 |
| $\mathrm{O}(1)-\mathrm{O}(2)$ | $2 \cdot 364$ (1) |
| -O(2') | $2 \cdot 440$ (2) |
| -O(2") | 2.409 (2) |
| $\mathrm{O}(2)-\mathrm{O}\left(2^{\prime}\right)$ | 2.428 (2) |
| $-\mathrm{O}\left(2^{\prime \prime}\right)$ | $2 \cdot 394$ (1) |
| $\mathrm{O}\left(2^{\prime}\right)-\mathrm{O}\left(2^{\prime \prime}\right)$ | $2 \cdot 388$ (2) |
| B-B' | 2.569 (5) |
| $-\mathrm{B}^{\prime \prime}$ | 2.664 (3) |
| $-\mathrm{B}^{\prime \prime \prime}$ | 2.664 (3) |
| - $\mathrm{B}^{\prime \prime \prime \prime}$ | 2.592 (3) |
| $\mathrm{O}(1)-\mathrm{B}-\mathrm{O}(2)$ | $110.2(2)^{\circ}$ |
| -O(2') | $115 \cdot 8$ (2) |
| -O(2') | $113 \cdot 1$ (2) |
| $\mathrm{O}(2)-\mathrm{B}-\mathrm{O}\left(2^{\prime}\right)$ | $107 \cdot 4$ (2) |
| -O(2') | $104 \cdot 9$ (2) |
| $\mathrm{O}\left(2^{\prime}\right)-\mathrm{B}-\mathrm{O}\left(2^{\prime \prime}\right)$ | $104 \cdot 7$ (1) |
| O-B-O (ave) | $109 \cdot 4$ |
| $\mathrm{B}-\mathrm{O}(1)-\mathrm{B}^{\prime}$ | $138 \cdot 6$ (3) |
| $\mathrm{B}-\mathrm{O}(2)-\mathrm{B}^{\prime \prime}$ | $123 \cdot 8$ (2) |
| $\mathrm{B}-\mathrm{O}\left(2^{\prime \prime}\right)-\mathrm{B}^{\prime \prime \prime}$ | $123 \cdot 8$ (2) |
| $\mathrm{B}-\mathrm{O}\left(2^{\prime}\right)-\mathrm{B}^{\prime \prime \prime \prime}$ | 118.7 (2) |

Symmetry transformations: $\mathrm{B}^{\prime}(x, \bar{y}, z), \mathrm{B}^{\prime \prime}\left(\frac{1}{2}+x, \frac{1}{2}-y, z\right)$, $\mathrm{B}^{\prime \prime \prime}\left(-\frac{1}{2}+x, \frac{1}{2}-y, z\right), \mathrm{B}^{\prime \prime \prime \prime}\left(\frac{1}{2}-x, \frac{1}{2}-y,-\frac{1}{2}+z\right), \mathrm{O}\left(2^{\prime}\right)\left(\frac{1}{2}-x\right.$, $\left.\frac{1}{2}-y,-\frac{1}{2}+z\right), \mathrm{O}\left(2^{\prime \prime}\right)\left(-\frac{1}{2}+x, \frac{1}{2}-y, z\right)$.

Final equivalent isotropic temperature factors (Hamilton, 1959) of 0.45 for $\mathrm{B}, 0.55$ for $\mathrm{O}(1)$, and 0.49 for $\mathrm{O}(2)$ are comparable to those obtained by Zachariasen (1963a) in cubic metaboric acid and to those of many other boron-oxygen compounds (e.g. Clark, Appleman \& Christ, 1964). The thermal vibrations are not notably anisotropic. Perhaps the most significant result of the anisotropic refinement is that the major axis of $\mathrm{O}(1)$ is approximately parallel to $\mathbf{c}$ and almost bisects the $\mathrm{B}-\mathrm{O}(1)-\mathrm{B}^{\prime}$ angle (Fig. 1), whereas the major axis of $O(2)$ is approximately normal to the bisector
of the $\mathrm{B}-\mathrm{O}(2)-\mathrm{B}^{\prime \prime}$ angle. Although the calculated errors for the $B$ ellipsoid are large, the orientation of the major axis is roughly normal to the $\mathrm{B}-\mathrm{O}(1)$ direction which represents the shortest $\mathrm{B}-\mathrm{O}$ distance.

## Discussion of the structure

Fig. 1 shows a tetrahedral model of the $\mathrm{B}_{2} \mathrm{O}_{3}$ II structure. Although the refinement started from a point based on closest-packed oxygen atoms, the actual structure is distorted considerably from this arrangement. The tetrahedral linkage is similar to that in wurtzite $(\mathrm{ZnS})$ or $\mathrm{LiGaO}_{2}$ (Marezio, 1965) except that in $\mathrm{B}_{2} \mathrm{O}_{3}$ II, only two-thirds of the tetrahedra are occupied. Furthermore, interatomic distances and angles (Table 4) show the tetrahedra to be very distorted, with one short $\mathrm{B}-\mathrm{O}(1)$ distance of $1.373 \AA$ and three long $\mathrm{B}-\mathrm{O}(2)$ distances of $1 \cdot 507,1 \cdot 506$, and $1 \cdot 512 \AA$. The average $\mathrm{B}-\mathrm{O}$ distance is $1.475 \AA$, exactly that proposed by Zachariasen (1963b) as an average tetrahedral $B-O$ distance. The oxygen associated with the short $\mathrm{B}-\mathrm{O}$ distance is coordinated by only two boron atoms, whereas the other is coordinated by three borons. If electrostatic bond strengths are taken from Zachariasen's table of bond strength versus $\mathrm{B}-\mathrm{O}$ bond length, the net bond strength is 3.01 around $\mathrm{B}, 1.96$ around $O(1)$, and 2.03 around $O(2)$, thus showing that the distortions are necessary to balance the electrostatic charge in the crystal.

The average $\mathrm{O}-\mathrm{O}$ distance in the tetrahedra is about $2.40 \AA$, resulting in $\mathrm{B}-\mathrm{O}(1)-\mathrm{B}$ angles of 138.6 and $\mathrm{B}-\mathrm{O}(2)-\mathrm{B}$ angles averaging $122^{\circ}$. The average tetrahedral $\mathrm{O}-\mathrm{B}-\mathrm{O}$ angle is $109 \cdot 4^{\circ}$.

It is difficult to tell whether the Berger (1953) $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$ structure is correct. In the assigned space group, $P 3_{1}$, there is only one equipoint, $3(a)$. Since $Z=3$, there are two B and three O locations. If the structure is tetrahedral, then two oxygen atoms must be coordinated by three boron atoms and the other oxygen by two boron atoms. Berger's structure, based on Guinier and Seeman-Bohlin powder data, does contain such an arrangement, but the $\mathrm{B}-\mathrm{O}$ distances, which range from $1 \cdot 31$ to $2 \cdot 15 \AA$, are not reasonable. Furthermore the data have not been refined and Berger gives no $R$ value.

Marezio (1967) has suggested that, in analogy to the borates and metaboric acids, at least three $\mathrm{B}_{2} \mathrm{O}_{3}$ structures might be expected, one with $\mathrm{BO}_{4}^{5-}$ tetrahedra, one with $\mathrm{BO}_{3}^{3-}$ triangles, and one or more with mixed tetrahedra and triangles. Since the $\mathrm{B}_{2} \mathrm{O}_{3}$ II structure definitely consists of tetrahedra, it is possible that the hexagonal structure contains one boron in triangular and one in tetrahedral coordination. This structure would require that two oxygen atoms be coordinated by two boron atoms, and the other by three boron atoms. To carry the analogy further, the Cole \& Taylor (1935) cubic material could contain boron in triangular coordination with all the oxygen two-coordinated. The densities of the three compounds are consistent with this picture, with $3 \cdot 11,2 \cdot 56$, and $1.82 \mathrm{~g} . \mathrm{cm}^{-3}$ for $\mathrm{B}_{2} \mathrm{O}_{3}$

II, $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$, and the Cole \& Taylor material, respectively. A similar variation in density with coordination occurs in the metaboric acids.*

The structure of $\mathrm{B}_{2} \mathrm{O}_{3}$ glass has been studied by X-ray (Warren, Krutter \& Morningstar, 1936), nuclear magnetic resonance (Bray \& Silver, 1960), and infrared (Simon, 1960) techniques. Although some controversy about details exists, there is general agreement that in the glass structure the boron is triangularly coordinated. Since the density of $\mathrm{B}_{2} \mathrm{O}_{3}$ glass is only slightly larger than that of the cubic $\mathrm{B}_{2} \mathrm{O}_{3}$, there may be some relation between the two structures. That others have not been able to repeat the Cole \& Taylor experiments remains puzzling. Perhaps the starting materials are important. Kracek et al. (1938) found that the presence of cubic metaboric acid was necessary to initiate crystallization of $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$ from $\mathrm{B}_{2} \mathrm{O}_{3}$ glass.

It is interesting to note that in our relatively shortterm experiments, $\mathrm{B}_{2} \mathrm{O}_{3}$ II melts at $525-550^{\circ} \mathrm{C}$ without reverting to $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$. The exact melting temperature of $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{II}$ is in doubt since Mackenzie \& Claussen (1961) found $50 \%$ glass in a four-day run at $475^{\circ} \mathrm{C}$. However,

* After this paper was written, a report of a reinvestigation of $\mathrm{B}_{2} \mathrm{O}_{3}$ I became available (G.E. Gurr, P. W. Montgomery, C.D.Knutson, and B.T.Gorres, Crystal Structure of Trigonal $\mathrm{B}_{2} \mathrm{O}_{3}$, ACA meeting, Minneapolis, Minnesota, August 20-25, 1967). According to this report, boron is coordinated by three oxygen atoms in $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$, thus nullifying the above argument for mixed coordinations in this compound. The possibility still exists that other $\mathrm{B}_{2} \mathrm{O}_{3}$ phases could be synthesized whose structures consist of mixed coordination geometries. It must be admitted, however, that the existence of only three-coordinated boron in the $\mathrm{B}_{2} \mathrm{O}_{3}$ I structure does add doubt to the validity of the Cole \& Taylor $\mathrm{B}_{2} \mathrm{O}_{3}$.
the melting point of $\mathrm{B}_{2} \mathrm{O}_{3}$ II is probably higher than that of $\mathrm{B}_{2} \mathrm{O}_{3} \mathrm{I}$ and considerably higher than that of the cubic material which melts at $294^{\circ} \mathrm{C}$.

The authors wish to acknowledge the help of Mr C. L. Hoover for performing the high-pressure experiments, Dr J. F. Whitney, Miss M.S. Licis and Mr E.P. Moore for assistance in obtaining the X-ray data, and Mr J. L. Gillson for performing the resistivity measurements. We also wish to thank Prof. D. R. Uhlmann and Mr R.L. Mozzi of Massachusetts Institute of Technology for valuable comments on the $\mathrm{B}_{2} \mathrm{O}_{3}$ system.

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Fig. I. The $\mathrm{B}_{2} \mathrm{O}_{3}$ II structure. The direction of $\mathbf{c}$ is down, into the page.

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# The Crystal Structure of $\mathbf{R e C l}_{5}$ 

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(Received 10 July 1967)


#### Abstract

$\mathrm{ReCl}_{5}$ forms monoclinic crystals with lattice constants: $a=9 \cdot 24, b=11 \cdot 54, c=12 \cdot 03 \AA ; \beta=109 \cdot 1^{\circ}$. The space group is $P 2_{1} / c$, and the unit cell contains eight $\mathrm{ReCl}_{5}$ units. Full-matrix, least-squares refinement of diffractometrically measured X-ray diffraction data resulted in a final $R$ of $9.3 \%$ (all reflections). The structure is based on a double-hexagonal closest packing of chlorine atoms, in which rhenium atoms occupy one-fifth of the octahedral holes. Two such octahedra share an edge to form a dimeric $\mathrm{Re}_{2} \mathrm{Cl}_{10}$ unit. The $\mathrm{Re}-\mathrm{Cl}$ bond distances involving bridging Cl average to $2.465 \pm 0.013 \AA$; the average bond length to nonbridging Cl is $2 \cdot 244 \pm 0.012 \AA$. Rhenium atoms in the $\mathrm{Re}_{2} \mathrm{Cl}_{10}$ units are each shifted by about $0.20 \AA$ from the centers of the octahedra in directions away from one another. The packing mode of Cl in $\mathrm{ReCl}_{5}$ contrasts with a hexagonal closest packing of Cl in $\mathrm{TaCl}_{5}$ and a cubic closest packing of Cl in $\mathrm{UCl}_{5}$. Of these, $\mathrm{ReCl}_{5}$ exhibits both the highest density and the smallest interatomic distances.


## Introduction

Four compounds in the rhenium-chlorine system are known (Colton, 1965): $\mathrm{ReCl}_{3}, \mathrm{ReCl}_{4}, \mathrm{ReCl}_{5}$ and $\mathrm{ReCl}_{6}$. The pentachloride is a dark brown to black material, melting at $220^{\circ} \mathrm{C}$. It is moisture-sensitive and highly reactive; a few of its chemical reactions have recently been investigated (Cotton, Robinson \& Walton, 1967).

Our interest in $\mathrm{ReCl}_{5}$ stems from the variety of crystal structures assumed by the pentachlorides. Examples include: ionic structures $-\mathrm{PCl}_{4}^{+}$and $\mathrm{PCl}_{6}^{-}$in $\mathrm{PCl}_{5}$ (Powell, Clark \& Wells, 1940); trigonal, bipyramidal molecules - $\mathrm{SbCl}_{5}$ (Ohlberg, 1959); bridged $\mathrm{M}_{2} \mathrm{Cl}_{10}$ dimers - $\mathrm{NbCl}_{5}$ (Zalkin \& Sands, 1958); $\mathrm{MoCl}_{5}$ (Sands \& Zalkin, 1959); $\mathrm{UCl}_{5}$ (Smith, Johnson \& Elson, 1967); and infinite chains of edge-shared pentagonal bipyramids $-\mathrm{PaCl}_{5}$ (Dodge, Smith, Johnson \& Elson, 1967). Five-coordination, we note, is avoided in all except $\mathrm{SbCl}_{5}$. The present investigation shows $\mathrm{ReCl}_{5}$ to be of the bridged-dimer type, but of a different crystallographic variety.

## Experimental

Our sample of $\mathrm{ReCl}_{5}$ was kindly provided by Dr D. Brown of the Atomic Energy Research Establishment, Harwell, England. Dr Brown informed us that the material was prepared by the thermal decomposition
of $\mathrm{ReCl}_{6}$ in a dry nitrogen atmosphere. Microscopic examination of the sample-tube showed a number of suitably sized crystals. The tube was opened in a drybox and a half-dozen or so crystals were sealed off in thin-walled glass capillaries for X-ray examination. The reactive nature of $\mathrm{ReCl}_{5}$ was evidenced by the fact that samples left open overnight in the dry-box developed traces of a brown liquid (possibly $\mathrm{ReOCl}_{4}$ ).

Single-crystal diffraction photographs showed monoclinic symmetry; the systematic extinctions ( $h 0 l, l=$ $2 n+1 ; 0 k 0, k=2 n+1$ ) are those uniquely characterizing the space group $P 2_{1} / c$ (International Tables for $X$-ray Crystallography, 1952). Refined values of the lattice constants are (Mo $K \alpha=0.7107 \AA$ ); $a=9 \cdot 24, b=$ $11 \cdot 54, c=12.03 \AA ; \beta=109 \cdot 1^{\circ}$ (probable errors estimated as about $0.3 \%$ ). The density calculated for eight $\mathrm{ReCl}_{5}$ units per unit cell is $3.98 \mathrm{~g} . \mathrm{cm}^{-3}$.

Intensity measurements were carried out on a General Electric XRD-5 diffractometer equipped with a goniostat. The crystal specimen was an irregularly shaped plate, approximately 0.22 mm in length and $0.14 \times 0.07 \mathrm{~mm}$ in cross section. The stationary crystalstationary counter technique (Furnas, 1957) was used; the radiation was Zr -filtered Mo $K \alpha$. A total of 1127 reflections were recorded up to a $2 \theta$-cutoff of $40^{\circ}$. Because of the irregular shape of the crystal and a rather large linear absorption coefficient $\left(\mu=233 \mathrm{~cm}^{-1}\right.$ for


[^0]:    * Contribution No. 1356.

[^1]:    * ASTM Powder Diffraction File, No. 13-570. This is reported as ' $99 \%$ pure, with water as impurity'. We find that the material in fact contains $39 \cdot 1 \mathrm{wt} . \%$ water. It could be a new form of $\mathrm{H}_{3} \mathrm{BO}_{3}$ which contains a calculated content of $43 \cdot 7 \%$ water.

